

1) Determine the following limits, if they exist:

a) $\lim_{x \rightarrow 1} \frac{x^a - 1}{x^b - 1}$. Also, what conditions must be put on a and b ?

b) $\lim_{x \rightarrow 0^+} \frac{\sin x}{1 - \cos x}$

c) $\lim_{x \rightarrow 1} \frac{e^{3x} - 1}{x}$

d) $\lim_{x \rightarrow 0} (\sin x)^{(\sin x)}$

2) A particle moves along the x -axis with acceleration function given by $a(t) = 4 - 3t^2$,
where a is in m/s when t is in s.

a) Find the most general anti-derivative of the function $a(t)$.

b) At $t = 0$, the velocity of the particle is 3 m/s. Determine its velocity at 2 s.

c) At $t = 0$ s, the particle is located at $x = 0$. Determine its position at 2 s.

3) The graph shows the velocity vs time graph for a particle moving along the x -axis, with time in s and velocity in m/s.

a) Estimate the displacement of the particle between 0 seconds and 6 seconds.

b) Estimate the total distance traveled by the particle between 0 seconds and 6 seconds.

c) Can you determine where the particle is at 6 s? If yes, do so, with supporting work. If not, explain why not.

